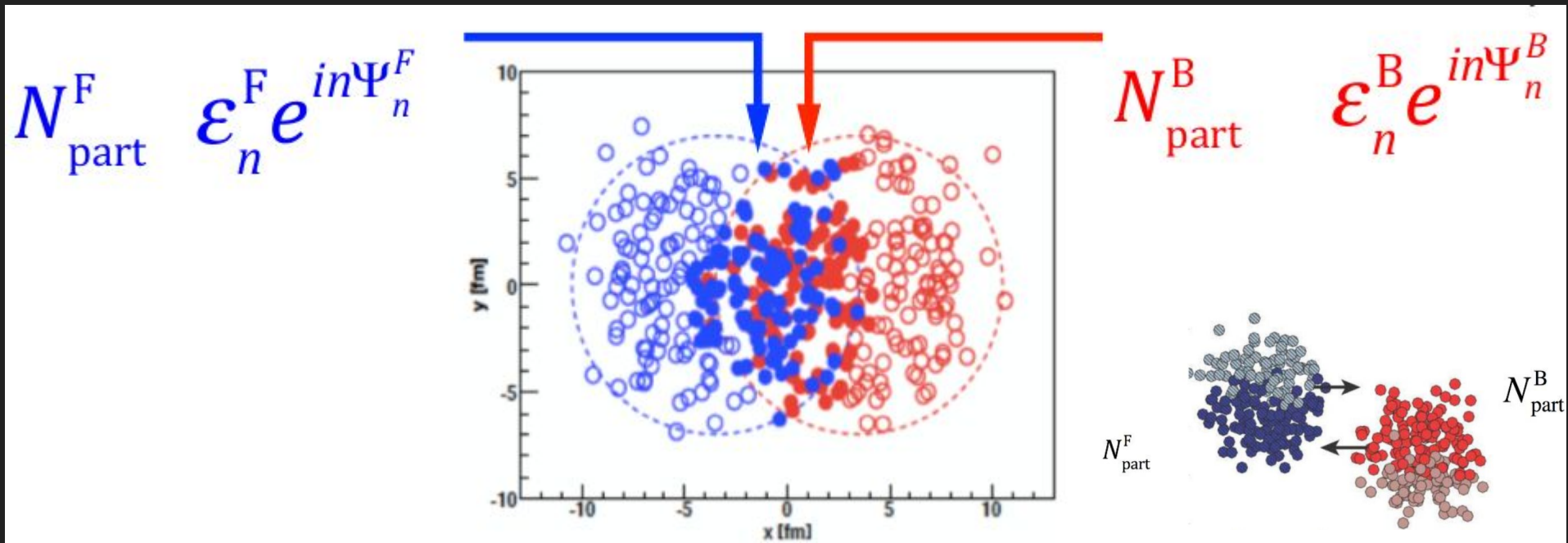


# Recent experimental results on Longitudinal multiplicity and flow fluctuations in heavy-ion collisions

Soumya Mohapatra  
(Columbia University)

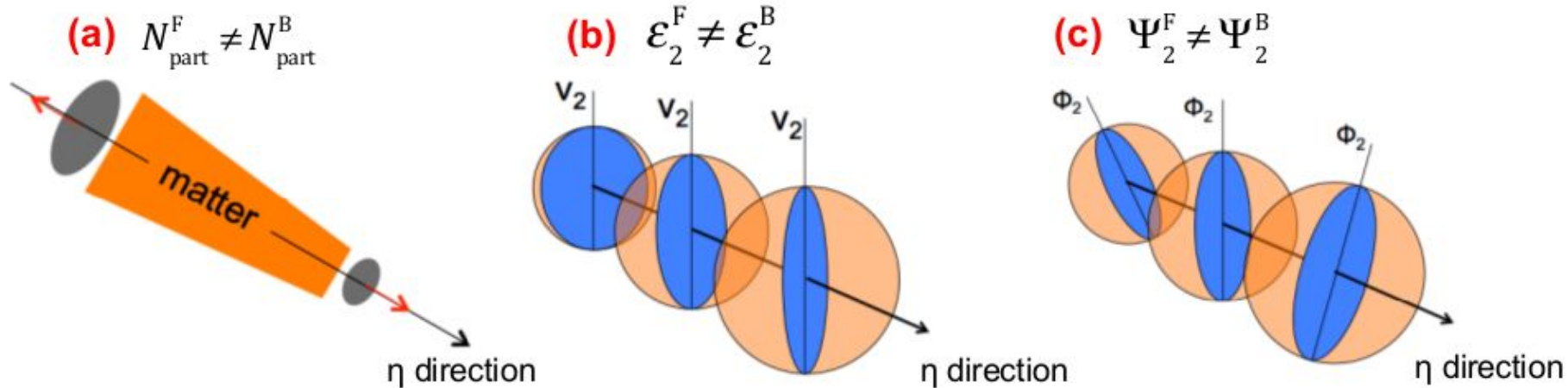
RHIC & AGS User's Meeting-2016

# Origin of longitudinal fluctuations



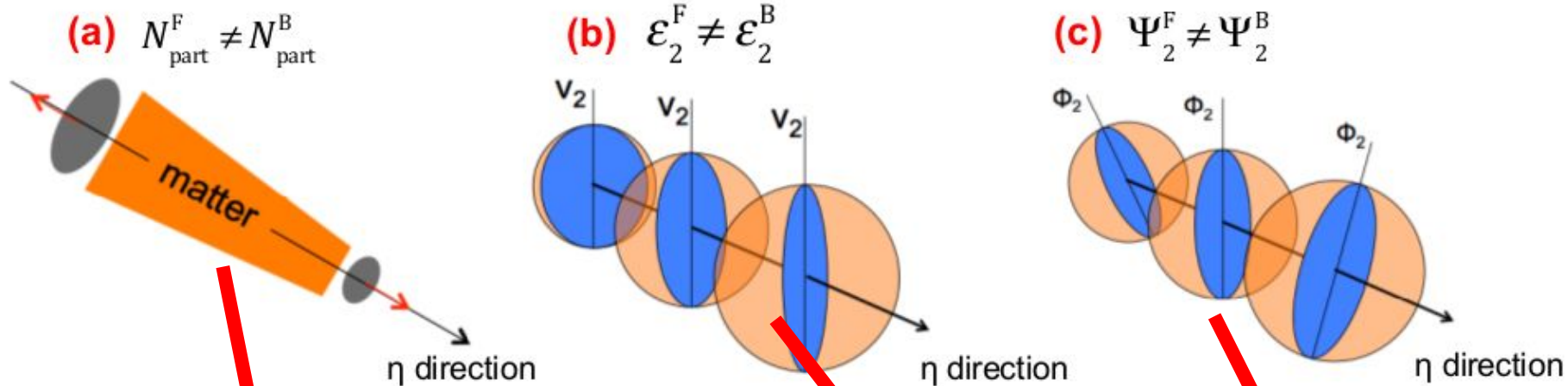
- Can see it in simple MC Galuber model picture
- Forward & backward going participant distributions are not symmetric

# Consequence of longitudinal fluctuations



- Forward & backward going participant distributions are not symmetric
- Three effects of asymmetry:
  - $N_{\text{part}}^F \neq N_{\text{part}}^B$
  - $\varepsilon_n^F \neq \varepsilon_n^B$
  - $\Psi_n^F \neq \Psi_n^B$

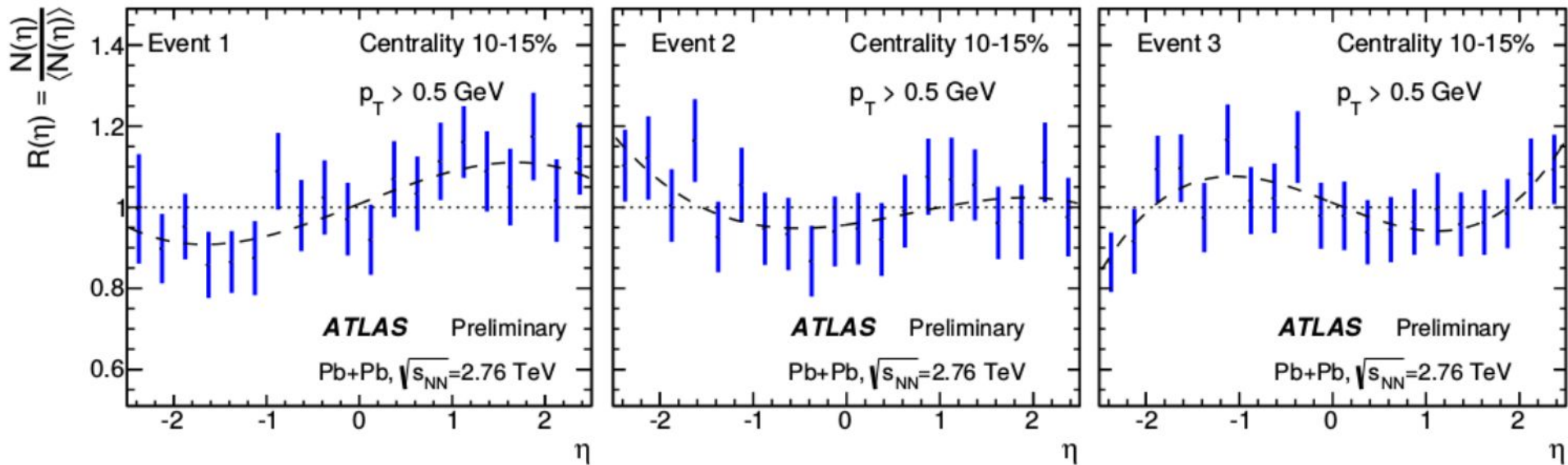
# Observing longitudinal fluctuations



Event-by-Event **Multiplicity**  
Fluctuations along  $\eta$ .  
(ATLAS)

EbE Flow fluctuations, in **magnitude** and **direction**  
along  $\eta$ . (CMS)

# EbE Forward-backward (FB) Multiplicity fluctuations



Event-by-Event single-particle multiplicity distributions (normalized):  $R_s(\eta) \equiv \frac{N(\eta)}{\langle N(\eta) \rangle}$

ATLAS-CONF-2015-020

- Observe clear multiplicity fluctuations along  $\eta$ .
- However single-particle observable cannot be easily used to study correlated fluctuations.

# Multiplicity correlation functions

Measure FB fluctuations using two-particle correlations

$$C(\eta_1, \eta_2) = \frac{\langle N(\eta_1)N(\eta_2) \rangle}{\langle N(\eta_1) \rangle \langle N(\eta_2) \rangle} \equiv \langle R_S(\eta_1)R_S(\eta_2) \rangle, \quad R_S(\eta) \equiv \frac{N(\eta)}{\langle N(\eta) \rangle}$$

ATLAS-CONF-2015-020  
ATLAS-CONF-2015-051

# Multiplicity correlation functions

Measure FB fluctuations using two-particle correlations

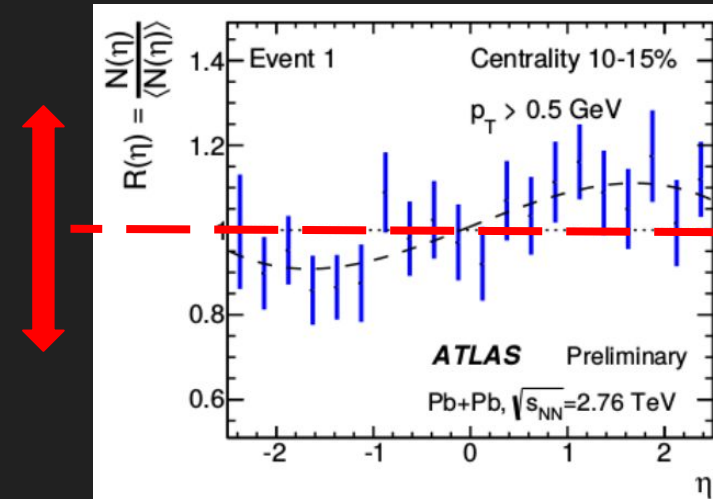
$$C(\eta_1, \eta_2) = \frac{\langle N(\eta_1)N(\eta_2) \rangle}{\langle N(\eta_1) \rangle \langle N(\eta_2) \rangle} \equiv \langle R_S(\eta_1)R_S(\eta_2) \rangle, \quad R_S(\eta) \equiv \frac{N(\eta)}{\langle N(\eta) \rangle}$$

ATLAS-CONF-2015-020  
ATLAS-CONF-2015-051

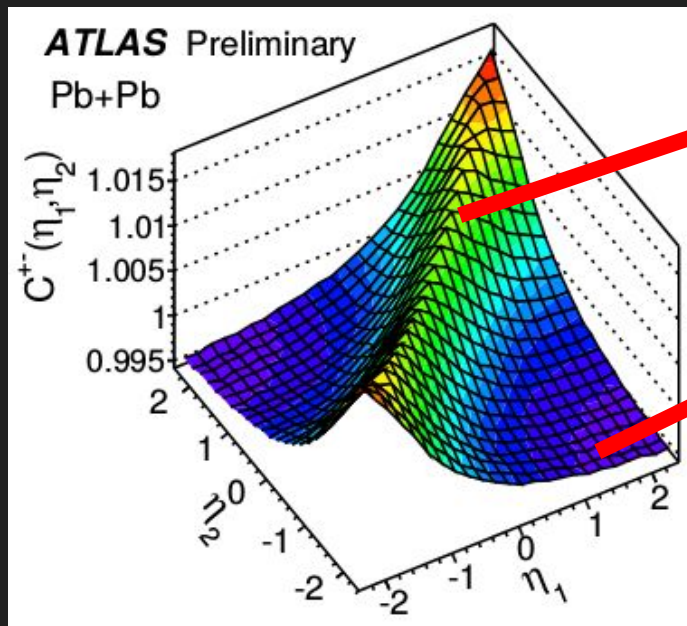
Renormalize to remove overall multiplicity fluctuations (single particle modes)

$$C_N(\eta_1, \eta_2) = \frac{C(\eta_1, \eta_2)}{C_p(\eta_1)C_p(\eta_2)},$$

$$C_p(\eta_1) = \frac{\int_{-Y}^Y C(\eta_1, \eta_2) d\eta_2}{2Y}, \quad C_p(\eta_2) = \frac{\int_{-Y}^Y C(\eta_1, \eta_2) d\eta_1}{2Y}$$



# Short-range correlations



Short-range correlations (Jets, decays) produce ridge-like structure along  $\eta_1 = \eta_2$ .

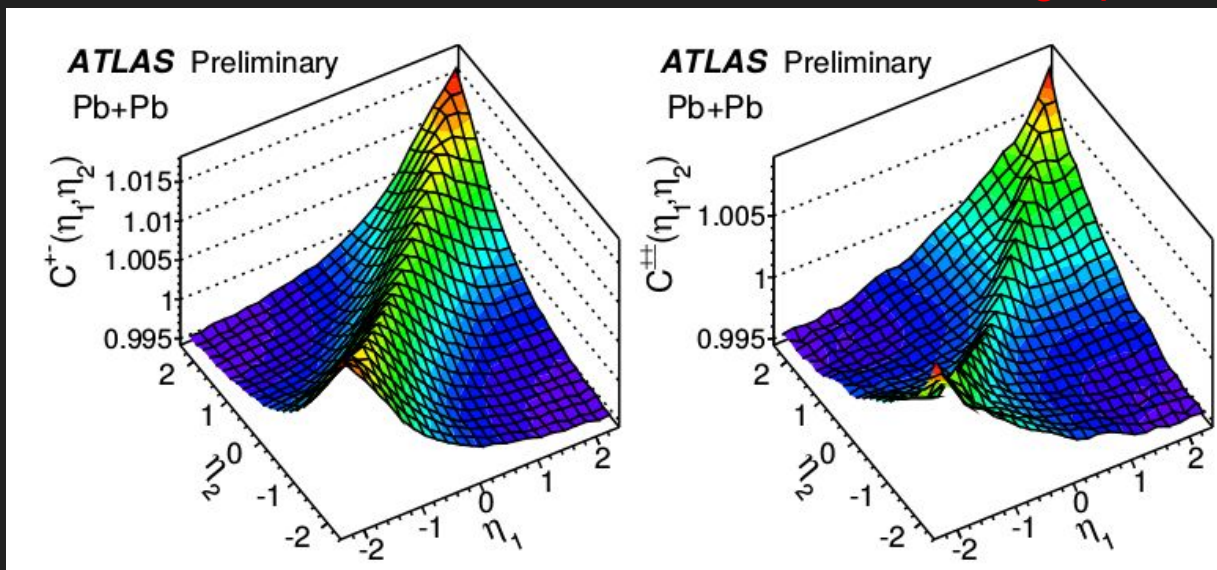
This must be removed first, before extracting features of the genuine long-range correlation that sits underneath



# Short-range correlations

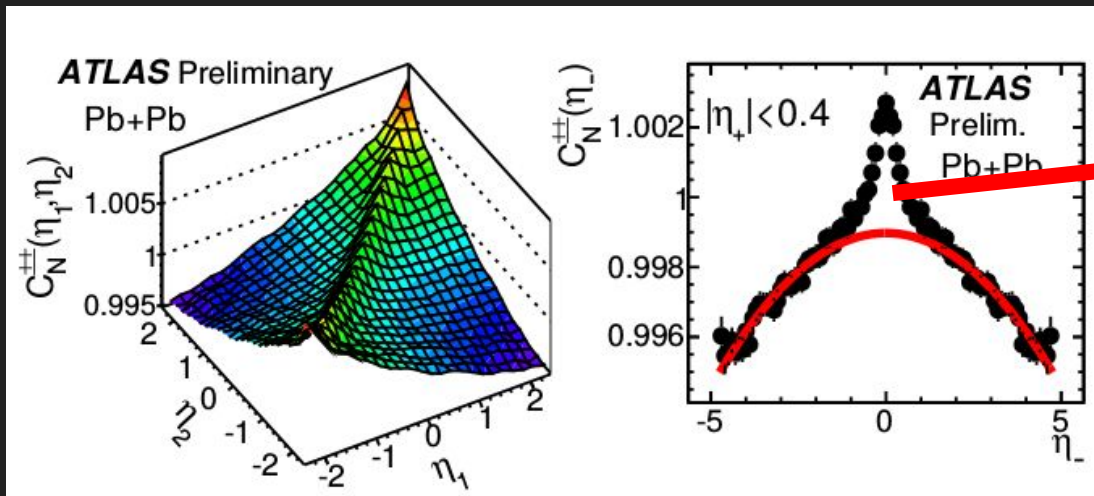
Opp-Charge pairs

Same-Charge pairs



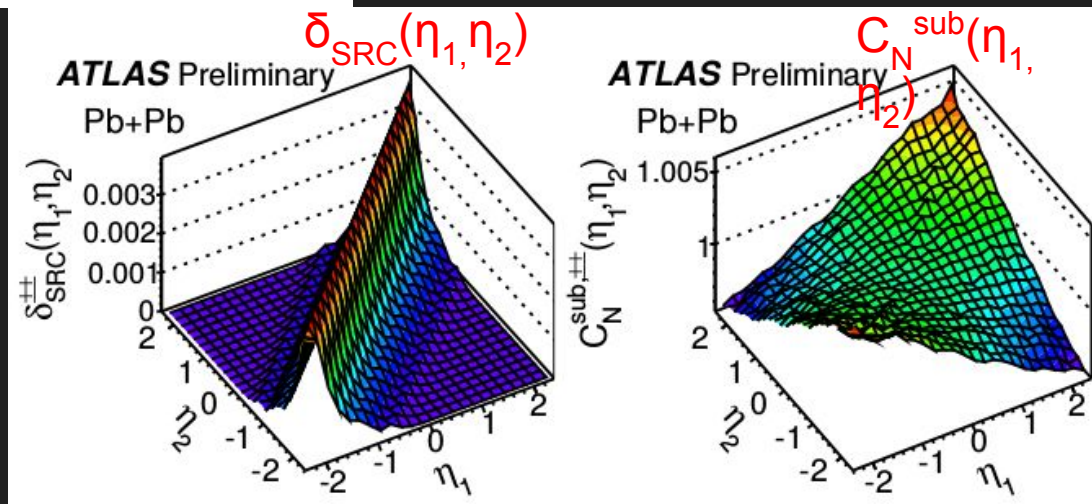
- Short-range correlations depend strongly on relative sign of particle pairs.
- Much larger for opposite-sign (left) than like sign pairs (right).
- Long range correlation quite identical!

# Short-range correlations : Removal



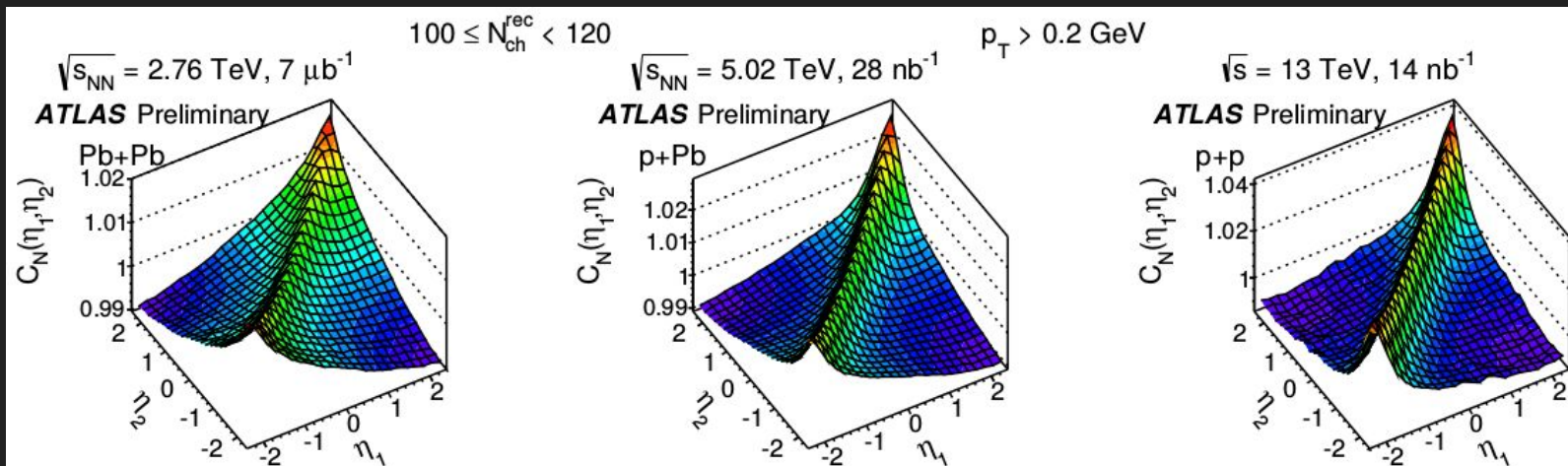
$$\delta_{\text{SRC}}(\eta_1, \eta_2)$$

- SRC is estimated by fitting 1D projection along  $\eta_1$ - $\eta_2$  with quadratic function over the range  $|\eta_1 - \eta_2| > 1.5$
- Excess over fit is assumed to be SRC and is removed
- Remaining correlation is the genuine long-range correlation:  $C_N^{\text{sub}}(\eta_1, \eta_2)$



# Extension to pp and p+Pb

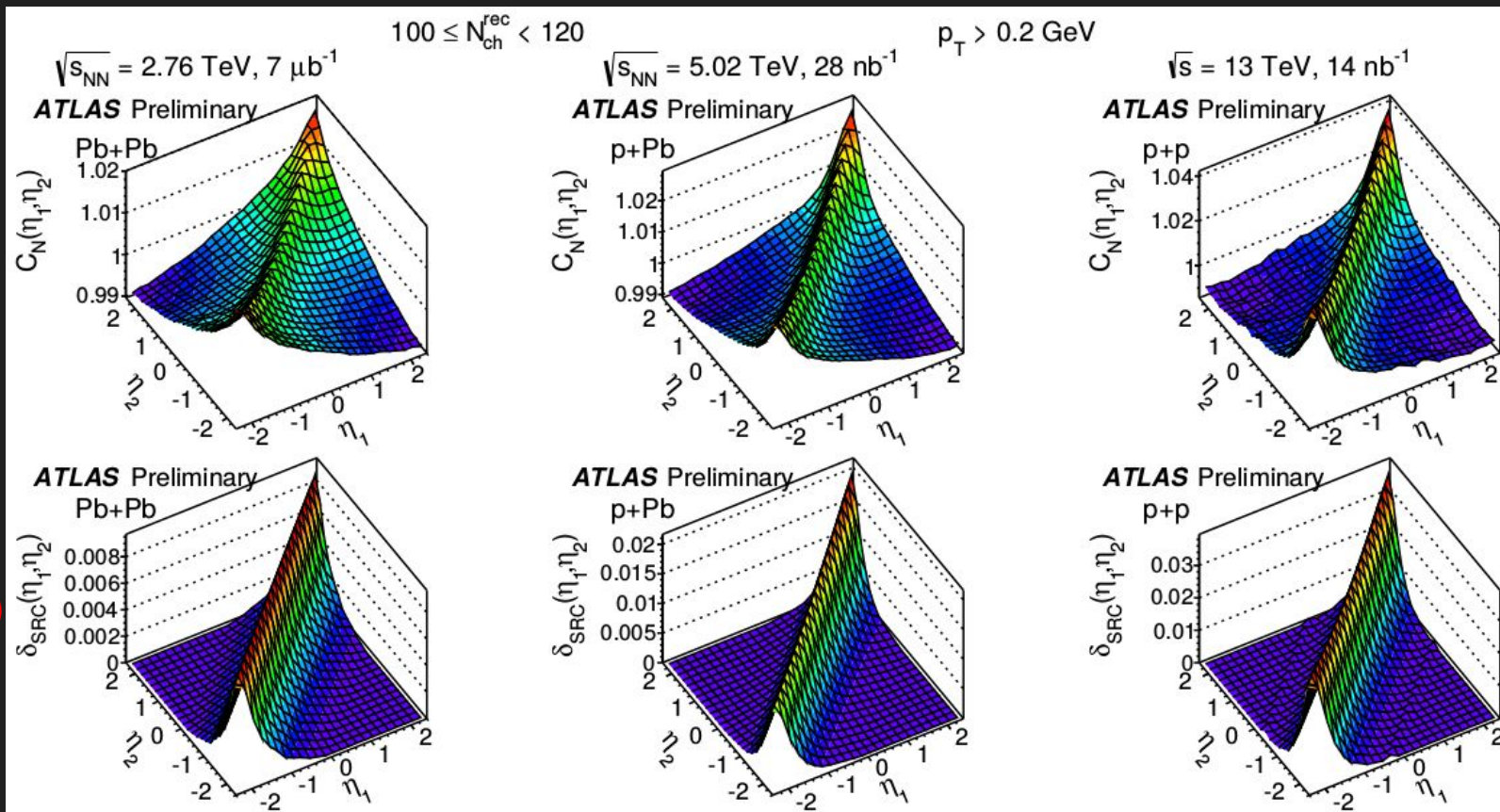
$C_N(\eta_1, \eta_2)$



# Extension to pp and p+Pb

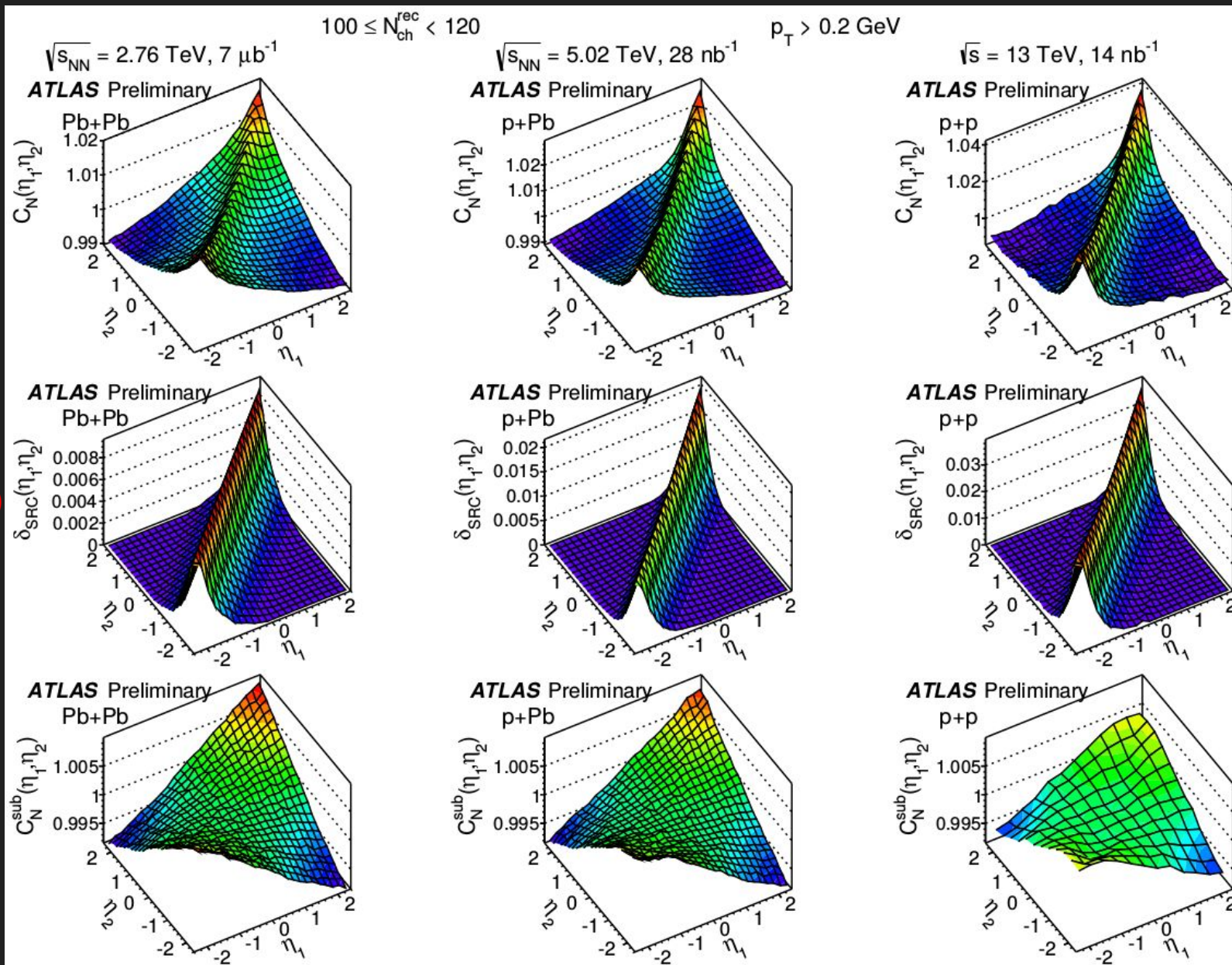
$$C_N(\eta_1, \eta_2)$$

$$\delta_{\text{SRC}}(\eta_1, \eta_2)$$





# Extension to pp and p+Pb



$C_N(\eta_1, \eta_2)$

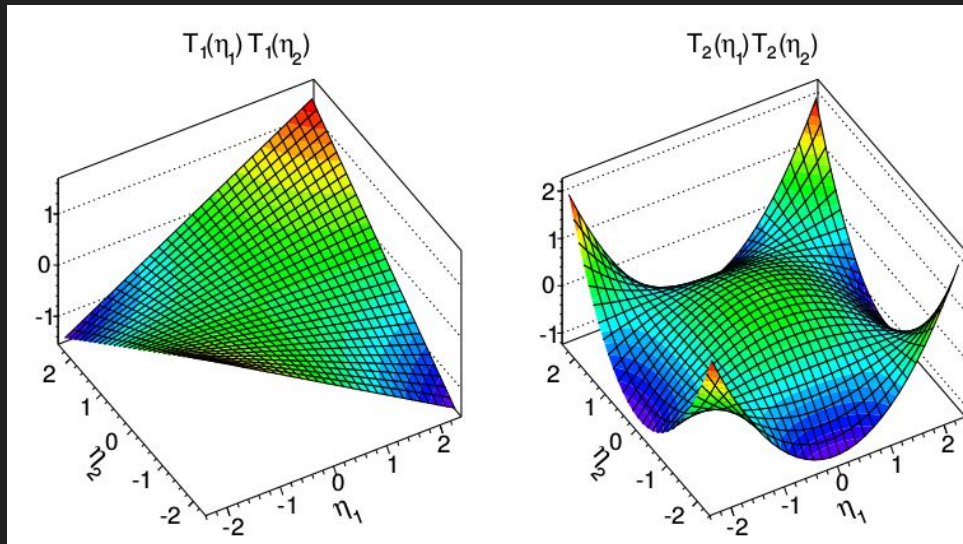
$\delta_{\text{SRC}}(\eta_1, \eta_2)$

$C_N^{\text{sub}}(\eta_1, \eta_2)$

# Quantifying the LRC

The LRC is quantified by expanding the correlation function in a 2D Legendre-function basis (arXiv:1210.1965: A. Bzdak, D.Teaney ):

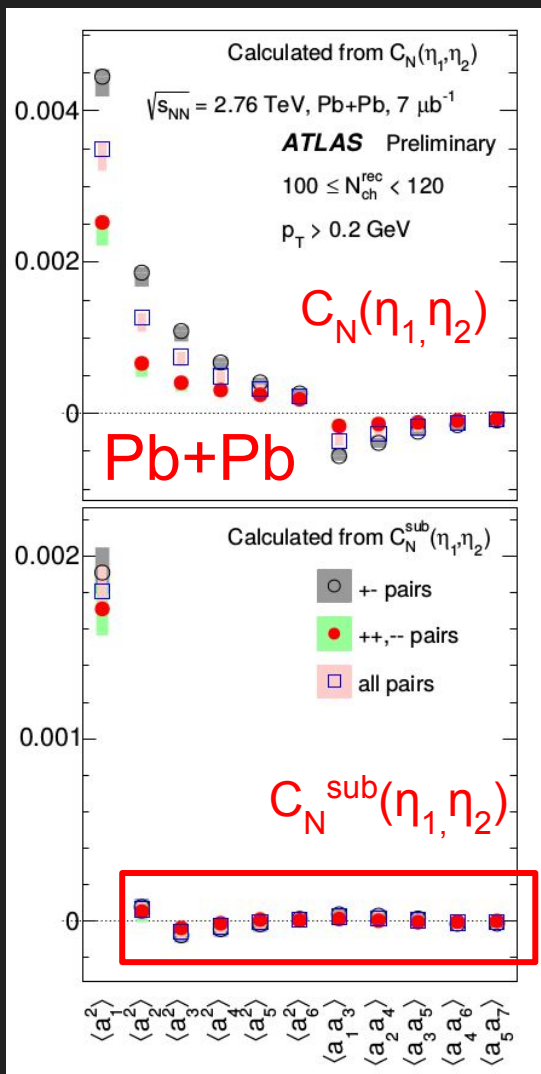
$$C_N(\eta_1, \eta_2) = 1 + \sum_{n,m=1}^{\infty} a_{n,m} \frac{T_n(\eta_1)T_m(\eta_2) + T_n(\eta_2)T_m(\eta_1)}{2}, \quad T_n(\eta) \equiv \sqrt{\frac{2n+1}{3}} Y P_n\left(\frac{\eta}{Y}\right)$$



Example basis functions  $T_1T_1$  and  $T_2T_2$

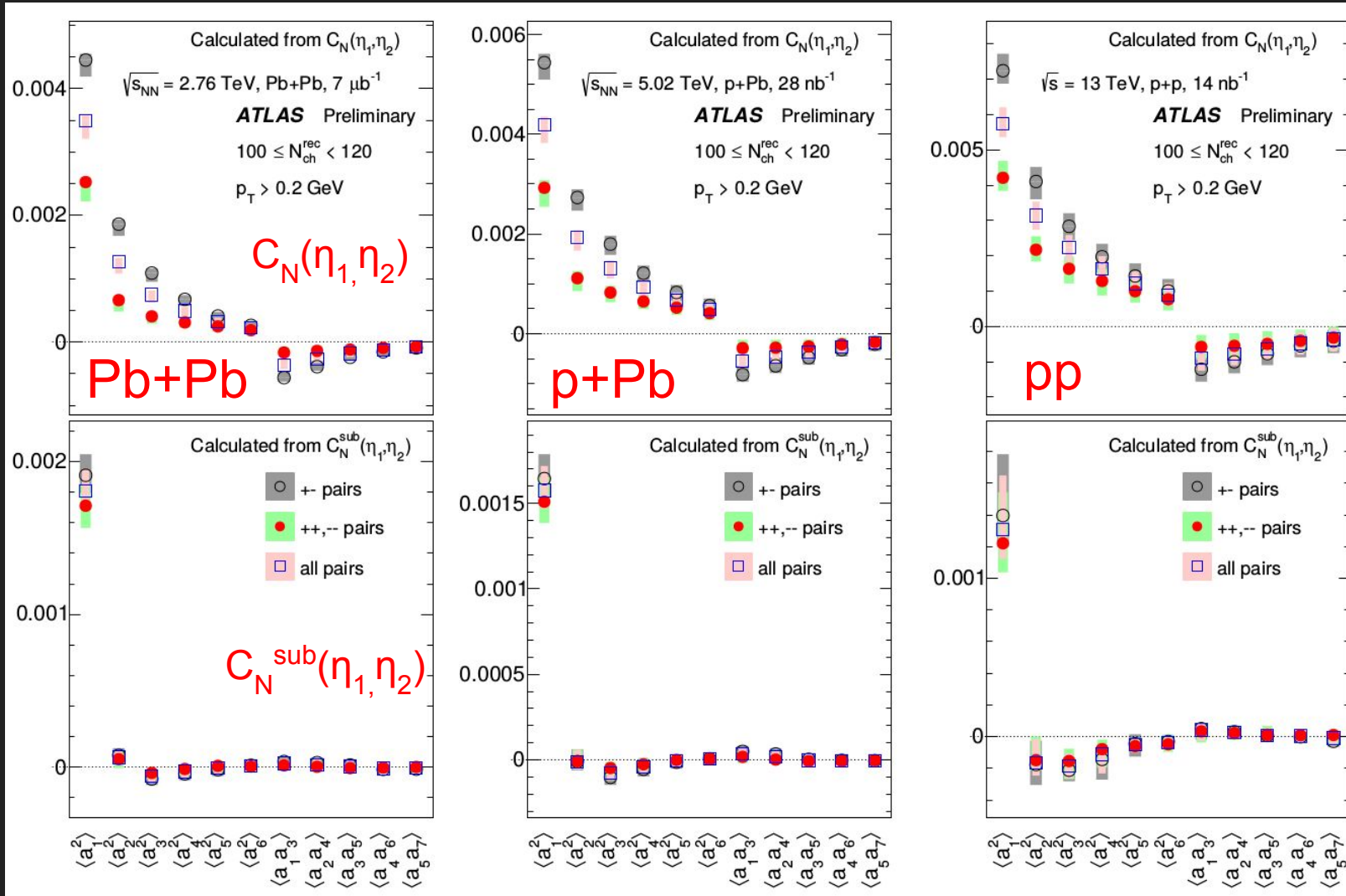
Coefficients of the expansion  $a_{m,n}$  quantify the correlation strength

# Correlation coefficients $a_{m,n}$



- Before SRC removal, several non-zero  $a_{m,n}$  are observed.
- Significant difference between same-charge and opposite charge pairs
- After SRC removal, only  $a_{1,1}$  is significant.
- FB fluctuation dominated by linear single-particle component
- Consistency between same-charge and opposite charge pairs

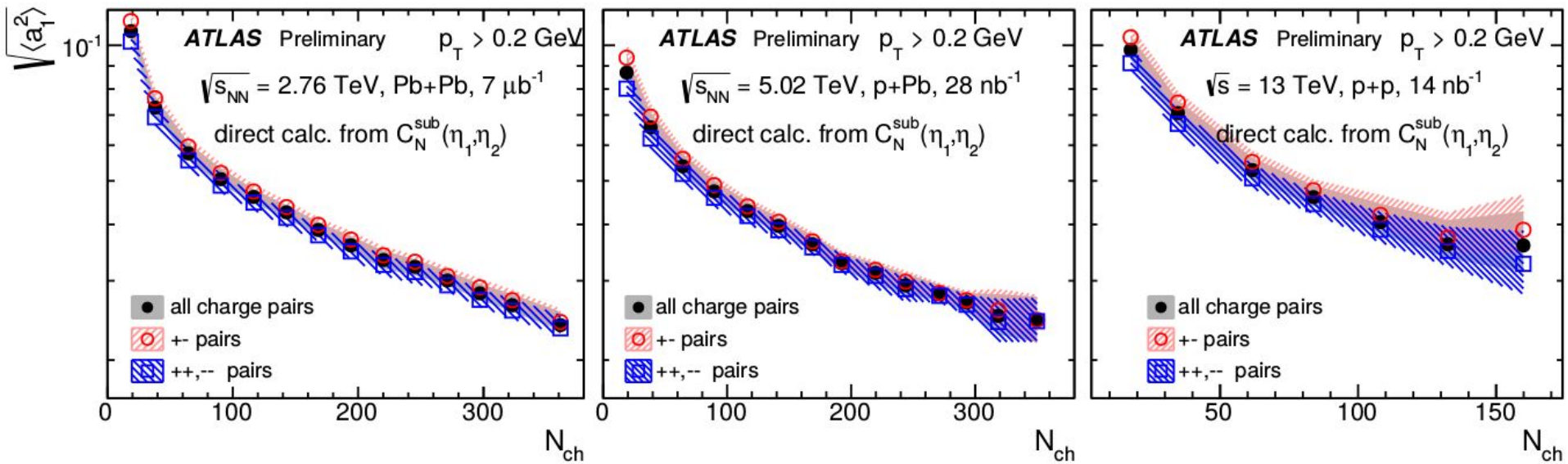
# $a_{m,n}$ : Dependence on colliding system



Same observation for pp and p+Pb

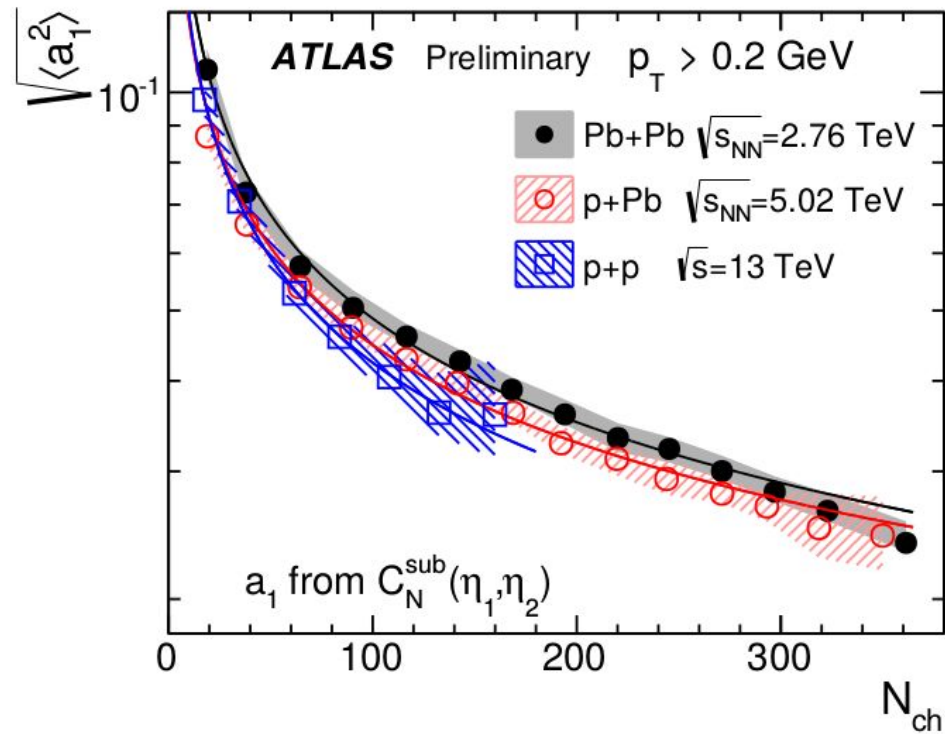
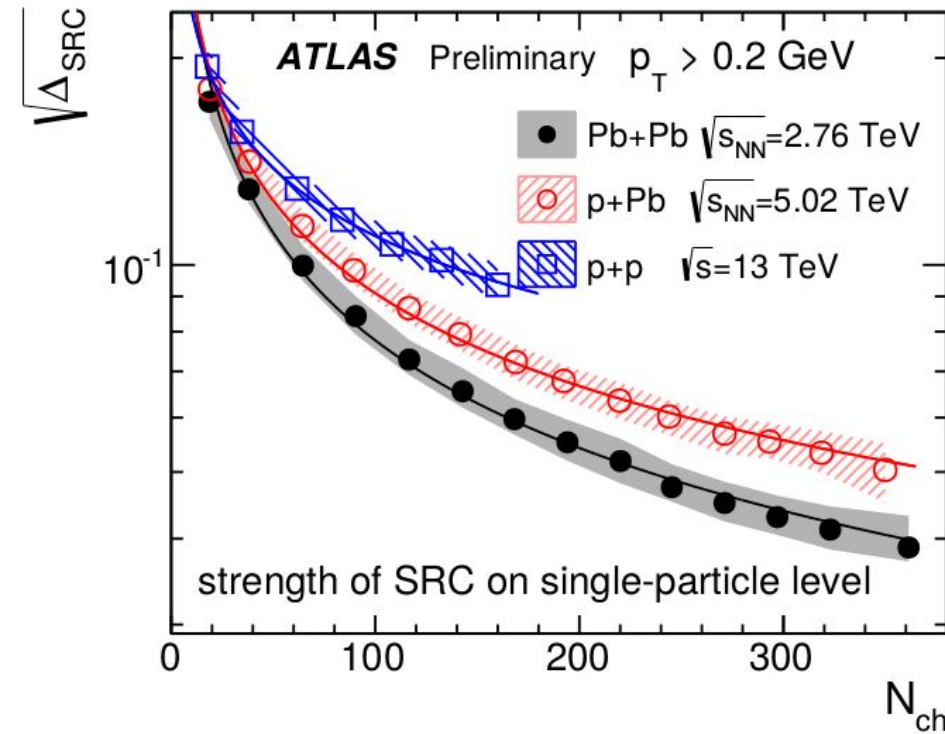


# Multiplicity dependence of $a_1$ :



- Decreases with increasing  $N_{ch}$ .
- Identical for different charge combinations across all multiplicities.
- Quite similar between pp, p+Pb and Pb+Pb (Note: different x-axis range)

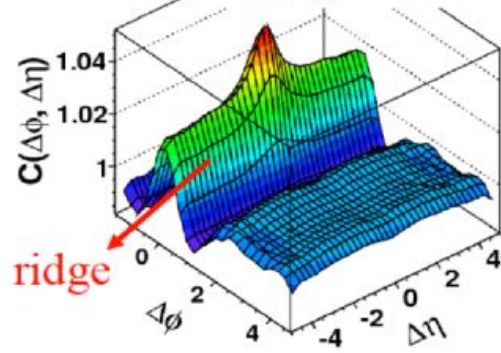
# SRC vs LRC



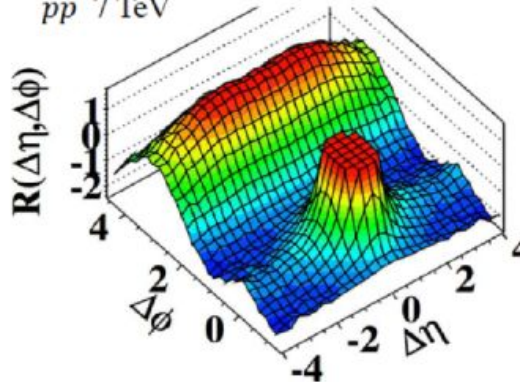
- SRC is quite different for the three systems
  - Largest for pp smallest for A+A (at same multiplicity)
- Quite comparable LRC for pp, pA and AA!

# Similarity of LRC for pp, p+Pb and Pb+Pb

Pb+Pb 2.76 TeV 0-5%  
ATLAS  $2 < p_T^a, p_T^b < 3$  GeV

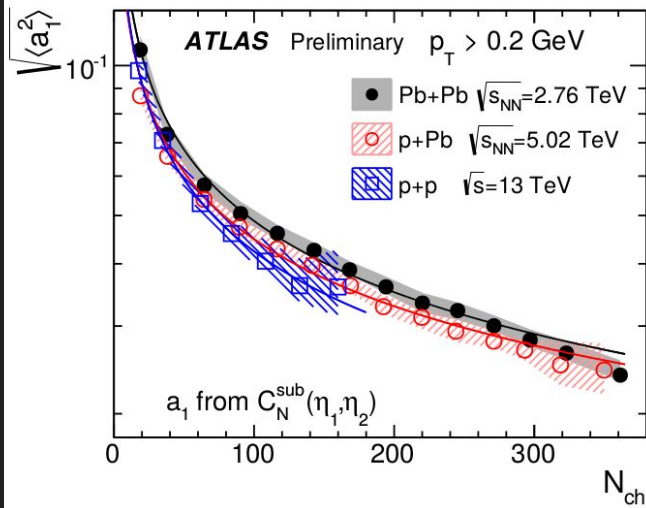
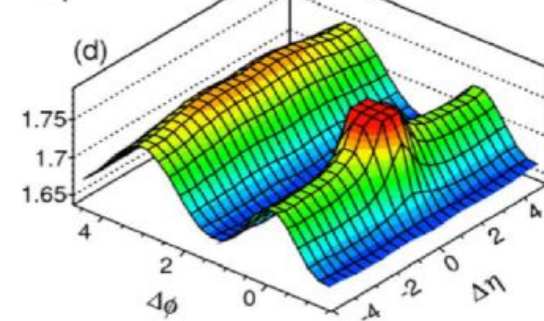


CMS  $N \geq 110, 1.0 \text{ GeV}/c < p_T < 3.0 \text{ GeV}/c$   
pp 7 TeV



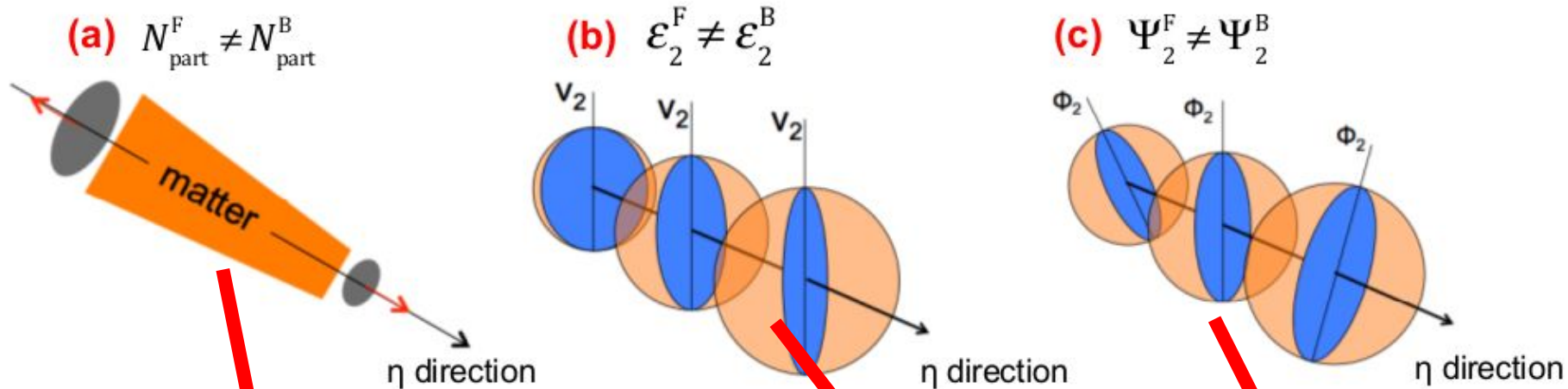
ATLAS p+Pb

$\sqrt{s_{NN}} = 5.02 \text{ TeV}, L_{int} \approx 28 \text{ nb}^{-1}$   
 $1 < p_T^{a,b} < 3 \text{ GeV}$   
 $N_{ch}^{rec} \geq 220$



pp, pA and AA are similar on multiple fronts!

# Longitudinal flow fluctuations

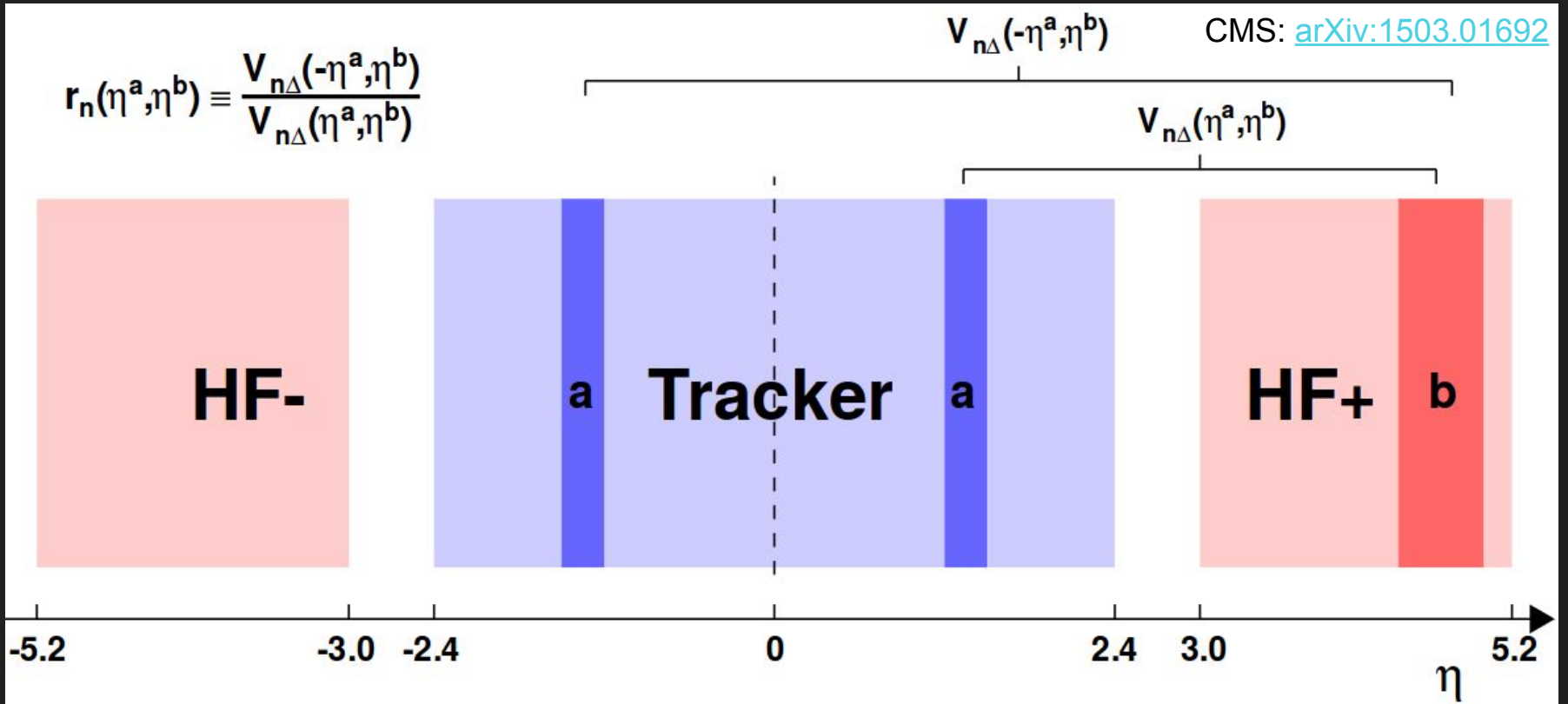


Event-by-Event **Multiplicity**  
Fluctuations along  $\eta$ .  
(ATLAS)

EbE Flow fluctuations, in **magnitude** and **direction**  
along  $\eta$ . (CMS)

# Quantifying the Event-plane rotation

$$v_{n\Delta}(\eta^a, \eta^b) = \langle v_n(\eta^a) v_n(\eta^b) \rangle \longrightarrow v_{n\Delta}(\eta^a, \eta^b) = \langle v_n(\eta^a) v_n(\eta^b) \cos(n\Psi_n(\eta^a) - n\Psi_n(\eta^b)) \rangle$$

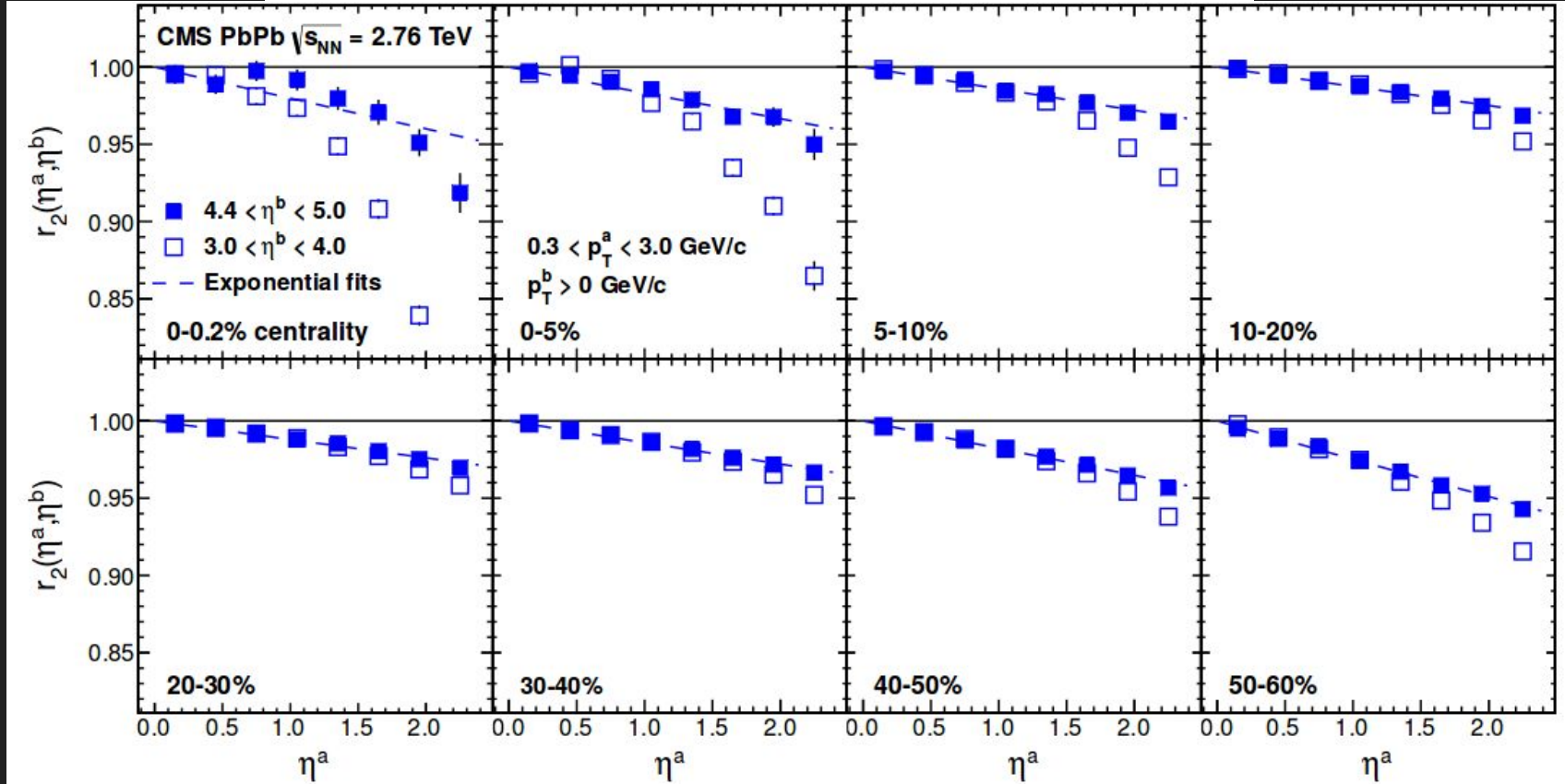


$$r_n(\eta^a, \eta^b) = \frac{\langle v_n(-\eta^a) v_n(\eta^b) \cos[n(\Psi_n(-\eta^a) - \Psi_n(\eta^b))] \rangle}{\langle v_n(\eta^a) v_n(\eta^b) \cos[n(\Psi_n(\eta^a) - \Psi_n(\eta^b))] \rangle} \sim \langle \cos[n(\Psi_n(\eta^a) - \Psi_n(-\eta^a))] \rangle$$



# Event-plane rotation: $\Psi_2$

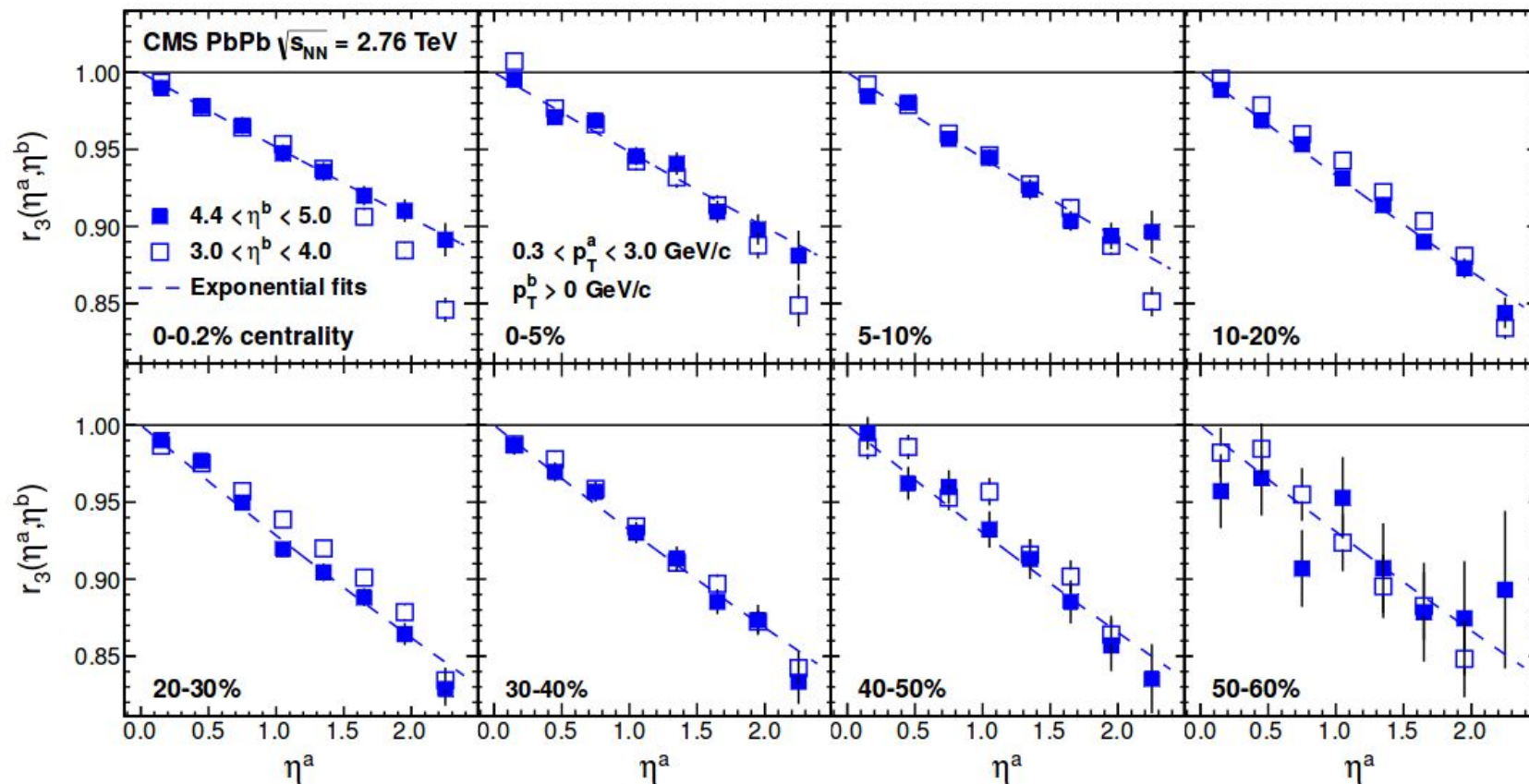
$$r_n \approx \left\langle \cos\left(n\Psi_n(\eta^a) - n\Psi_n(-\eta^a)\right) \right\rangle \approx e^{-2F_n^\eta \eta^a}$$



- Clear de-correlation (rotation) observed
- Observable has some dependence on choice of reference bin
  - Dependence is smaller in mid-central events and for  $\eta^a < 1$
- Effect decreases from central->mid-central then increases again

# Event-plane rotation: $\Psi_3$

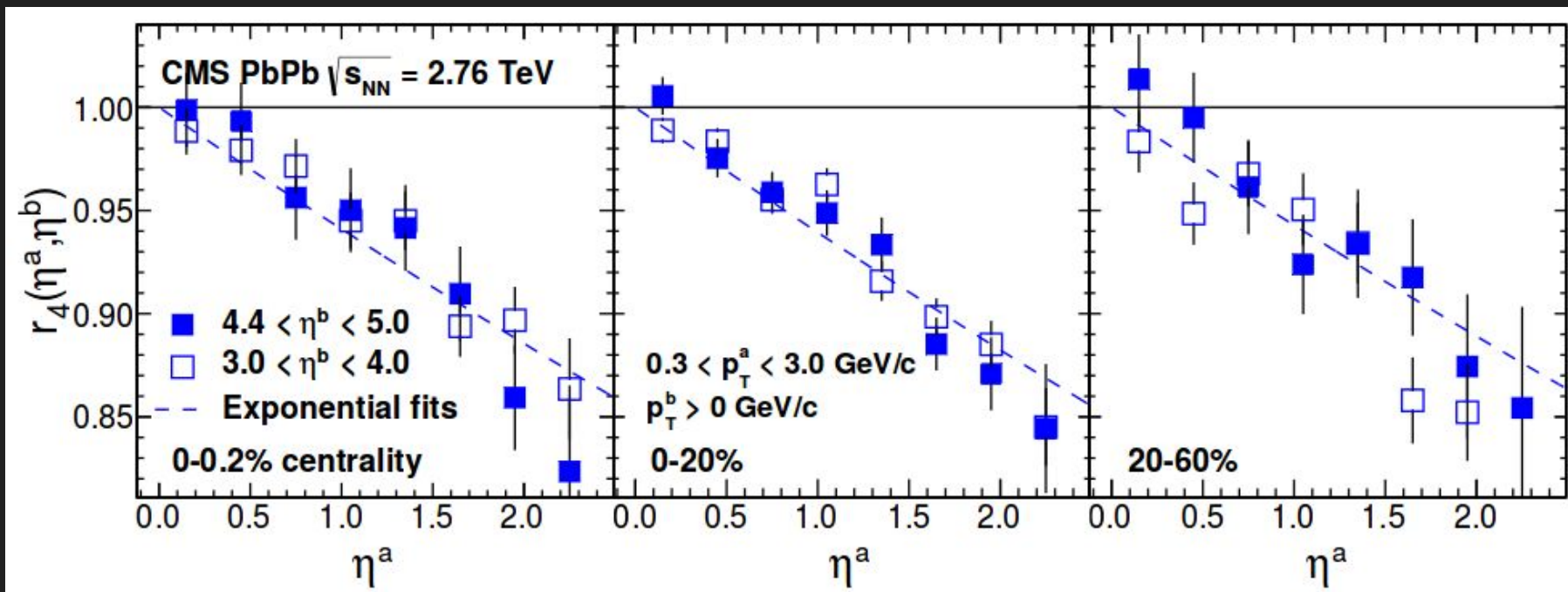
$$r_n \approx \left\langle \cos\left(n\Psi_n(\eta^a) - n\Psi_n(-\eta^a)\right) \right\rangle \approx e^{-2F_n^\eta \eta^a}$$



- Significantly larger rotation for  $n=3$
- Nearly independent of choice of reference bin
- Not much centrality dependence

# Event-plane rotation: $\Psi_4$

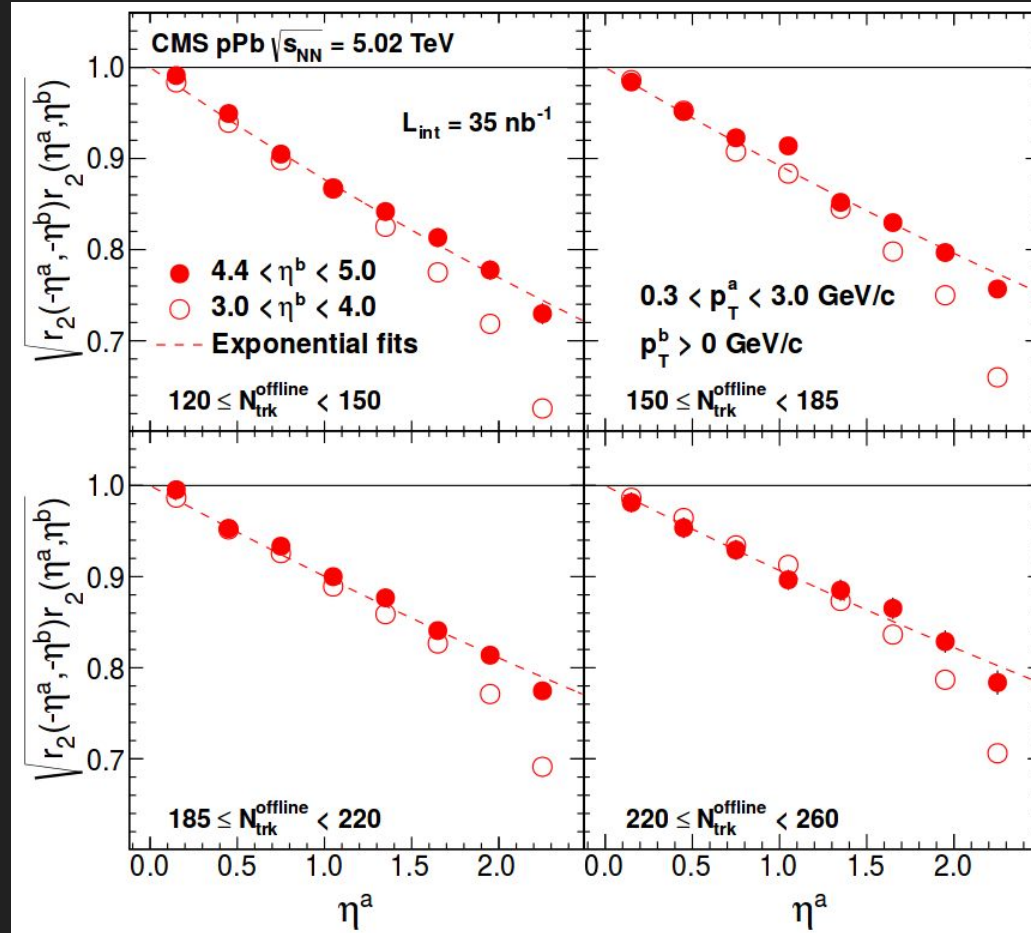
$$r_n \approx \left\langle \cos\left(n\Psi_n(\eta^a) - n\Psi_n(-\eta^a)\right) \right\rangle \approx e^{-2F_n^\eta \eta^a}$$



- Significantly larger rotation for  $n=4$  (compared to  $n=2$ )
- Nearly independent of choice of reference bin
- Not much centrality dependence

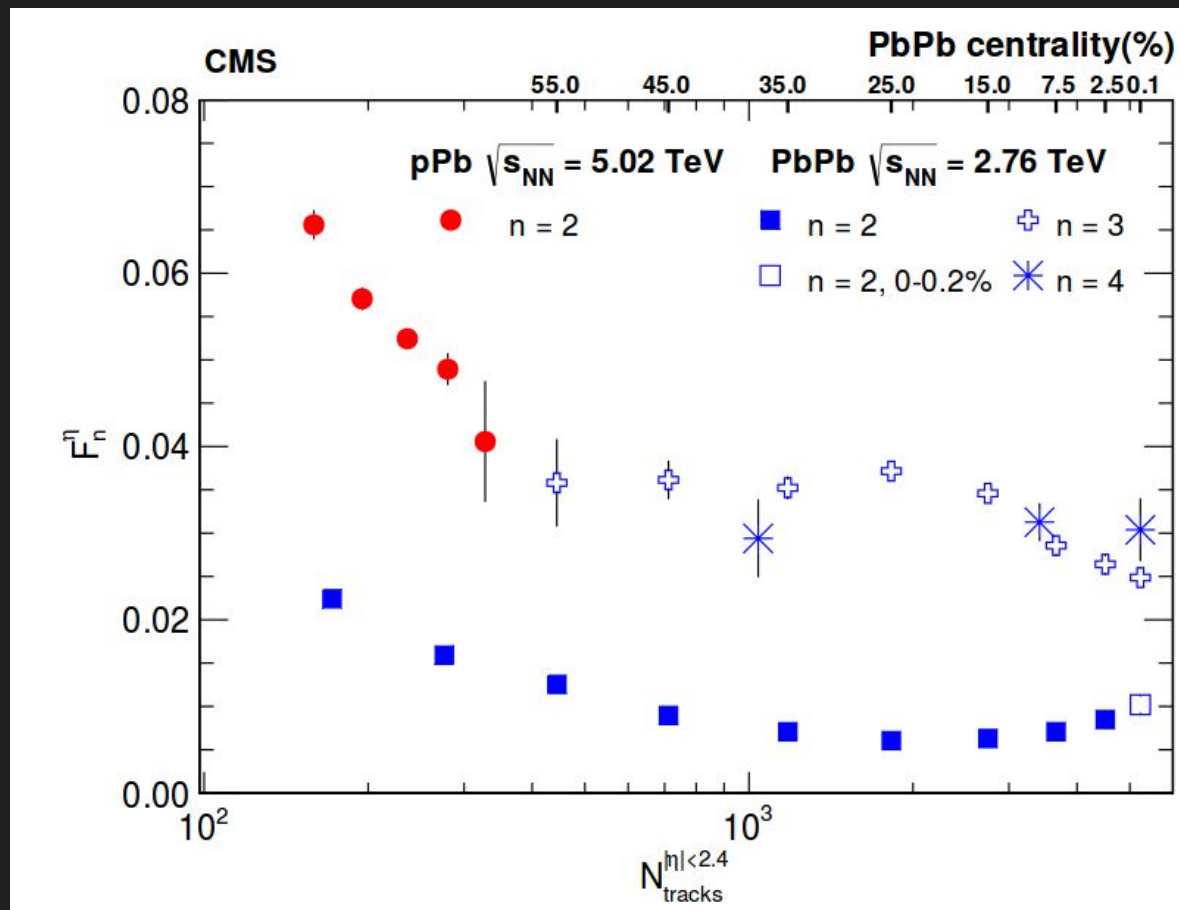


# Factorization breakdown in p+Pb: $\Psi_2$



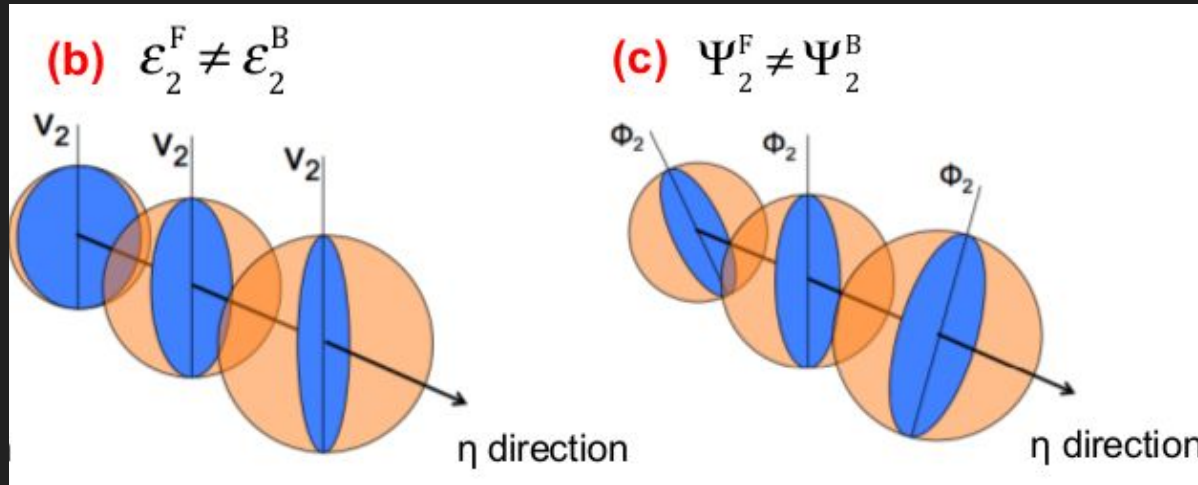
- Significantly larger rotation for p+Pb
- Nearly independent of choice of reference bin

# Event-plane de-correlations: summary



- For  $n=2$  first decreases then increases with centrality and harmonic order ' $n$ '
  - Interesting as  $p_T$  dependent factorization breakdown is larger for  $v_2$  than for  $v_3$
- No clear centrality dependence for  $n=4$
- Much larger in p+Pb compared to Pb+Pb at same multiplicity

# Drawback of the EP decorrelation measurement



$$r_n(\eta^a, \eta^b) = \frac{\left\langle v_n(-\eta^a) v_n(\eta^b) \cos[n(\Psi_n(-\eta^a) - \Psi_n(\eta^b))] \right\rangle}{\left\langle v_n(\eta^a) v_n(\eta^b) \cos[n(\Psi_n(\eta^a) - \Psi_n(\eta^b))] \right\rangle} \sim \left\langle \cos[n(\Psi_n(\eta^a) - \Psi_n(-\eta^a))] \right\rangle$$

- Cannot differentiate between magnitude fluctuation and EP rotation
- Interprets magnitude fluctuation effects as rotation effects

# Summary

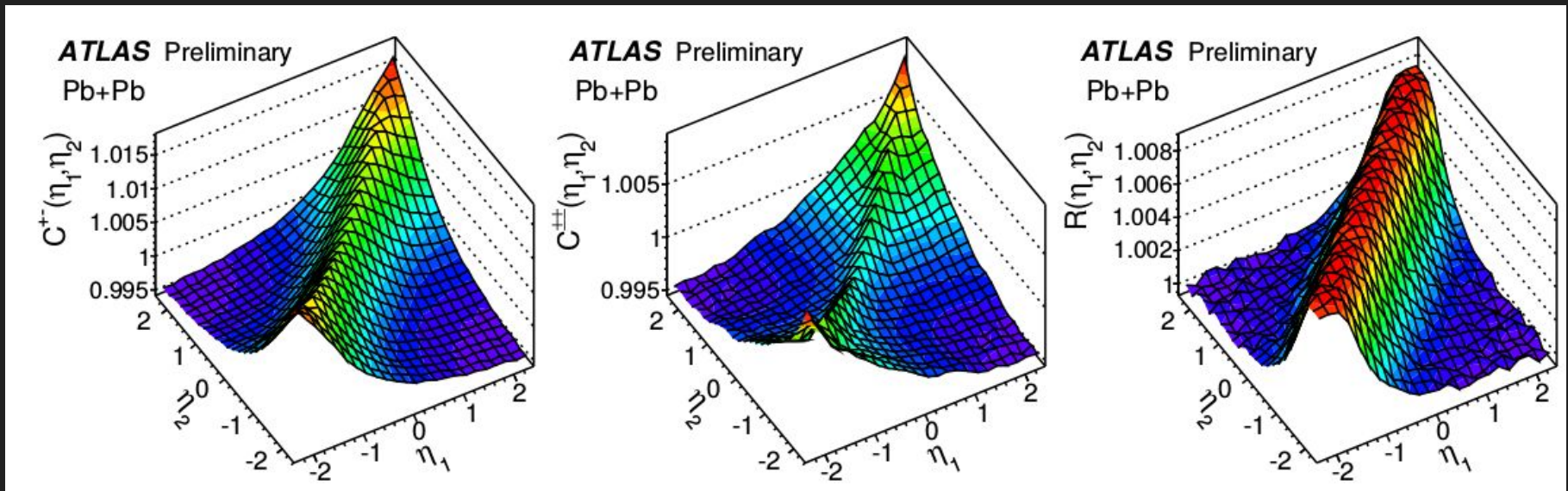
- Recently there has been much progress in studying longitudinal multiplicity and flow fluctuations (Both theory and experiment)
- Measurements include
  - FB Multiplicity correlations from ATLAS
  - EP rotation measurements from CMS
- FB Multiplicity correlations:
  - Linear multiplicity variation is dominant source.
  - Very similar correlations for pp, pA and AA collisions
  - Systems not too dissimilar after all?
- EP rotations
  - Significant rotation is observed increasing with harmonic order 'n'.
  - Larger for pA than for AA
  - Must develop observable to disentangle magnitude fluctuations from EP rotation
- Will be interesting to make these measurements in Cu+Au, d/He+Au systems at RHIC

# Short-range correlations : Estimation

Opp-Charge pairs

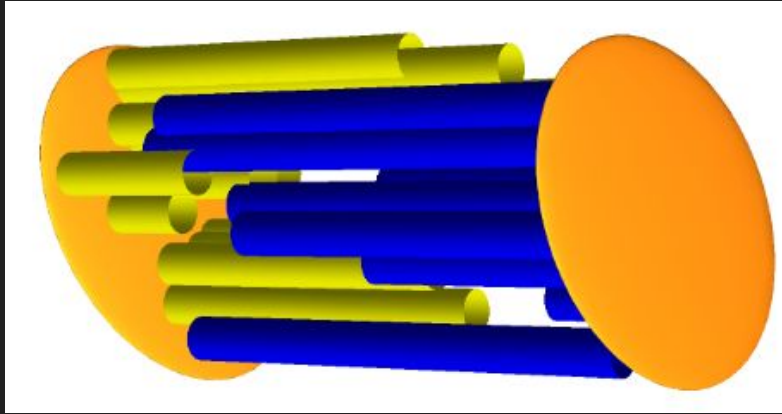
Same-Charge pairs

Ratio



- Short-range correlations depend strongly on relative sign of particle pairs
- Much larger for opposite-sign (left) than like sign pairs (right)
- Ratio has some interesting properties

# Other mechanisms of longitudinal fluctuations



Sources of fluctuating length along  $\eta$ .  
[arXiv:1512.01945](https://arxiv.org/abs/1512.01945) (W. Broniowski, P. Bozek)